## Lathe Electronic Edge Finder Model 1.5, version 0.1

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The LEEF Model 1.5 is almost identical to the Model 1 except for sensitivity. The Model 1 has an average threshold of 2.06 ohms. The Model 1.5 has an average threshold of 0.2 ohms. This increase in sensitivity comes at a cost. While the Model 1 uses less than 10 mA for its test current, the Model 1.5 uses less than 55 mA . There is a lot of shop experience with edge finders passing around 10 mA through the machine's bearings with no ill effects. There is also experience with currents greater than 1000 mA passing through bearings causing damage. The further we get away from 10 mA and the closer we get to 1000 mA , the more risk the operator takes. No scientific data has been found to assess the risk of a 55 mA test current.

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## Overview of Circuit

The circuit has automatic power control. When the test probes are connected to the machine, the circuit turns on. When the probes are disconnected, the circuit powers down.


This function is performed by having the test current pass through R2. This causes Q1 to be driven deep into saturation. Q1's collector is then pulled up to near 9 V which feeds the quad op amp.


The test current passing through R2 feeds into the unknown resistance, $\mathrm{R}_{\mathrm{x}}$ via probe A1. The current then flows out of $R_{x}$ via probe B1, into R3, and returns to ground.

Not shown in the scematic is that there is unknown contact resistance is these probes. This resistance can be almost as large as $\mathrm{R}_{\mathrm{x}}$ so has the potential of creating a large error. What makes this resistance troublesome is that the voltage across $\mathrm{R}_{\mathrm{x}}$ can be about the same as the voltage across contact A1 and/or B1.

We solve this problem by having a second set of probes, A2 and B2. These probes would have similar contact resistance but carry almost no current ${ }^{2}$. We therefore do not genarate much voltage across A2 or B2. While our test current flowing through A 1 and B 1 is around 50 mA , our current through A2 and B2 is around 30 nA which is 1 million times smaller.
$\mathrm{R}_{7}$ and $\mathrm{R}_{8}$ provide paths to ground for stray static electricity current that could damage the op amps. They have minimal effect on accuracy.

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Op amps A and B measure the voltage across $R_{x}$. When $R_{x}$ equals the threshold, the voltage at pin 1 equals the voltage at pin 7 . Below this threshold, the touchdown LED is red. Above this threshold it is green.


When $R_{x}$ is above the threshold, the voltage on pin 1 is greater than the voltage on pin 7. This causes op amp C to drive pin 8 to near 8 V while causing op amp D to drive pin 14 to near 0 volts. Current then flows from pin 8 to pin 14 causing the green LED to light.

When $R_{x}$ is below the threshold, the voltage on pin 1 is less than the voltage on pin 7. This causes op amp C to drive pin 8 to near 0 volts while causing op amp $D$ to drive pin 14 to near 8 V . Current then flows from pin 14 to pin 8 causing the red LED to light.

## Detailed Circuit Analysis


$I_{x}$ is the current through $R_{x}$

$$
\begin{equation*}
I_{x}=\frac{\left(V_{\text {battery }}-V_{E B s a t}\right)}{R_{2}+R_{x}+R_{3}} \tag{1}
\end{equation*}
$$

$I_{x}=\frac{(9 V-0.75 V)}{130+R_{x}+33}$
But since $R_{x}$ is much less than $133+33$ ohms, we can ignore it and say that
$I_{x} \cong \frac{(9 V-0.75 \mathrm{~V})}{133+33}$
$I_{x} \cong 50 \mathrm{~mA}$

$\mathrm{V}_{5}$ is the voltage at pin 5 with respect to ground.

$$
\begin{equation*}
V_{5}=R_{3} \times I_{x} \tag{3}
\end{equation*}
$$

This assumes that the input bias current flowing out of pin 5 is small. For the LT1014 it is equal to or less than 30 nA which is much less than $\mathrm{I}_{\mathrm{x}}$ of 50 mA so it is a reasonable assumption.

$$
\begin{equation*}
V_{3}=\left\{V_{5}\right\}+R_{x} I_{x} \tag{4}
\end{equation*}
$$

This ignores the input bias current flowing out of pin 3 .
Putting (3) into (4) we get

$$
V_{3}=\left\{R_{3} \times I_{x}\right\}+R_{x} I_{x}
$$

or

$$
\begin{equation*}
V_{3}=\left(R_{3}+R_{x}\right) \times I_{x} \tag{5}
\end{equation*}
$$

We now have the input voltages to op amps A and B defined.
Next we will look at the output of op amps A and B.


First consider op amp A in the ideal case. This op amp is configured for unity gain. The output voltage equals about $10^{5}$ times the input voltage. This means that the input voltage is $10^{-5}$ times the output voltage. So for any output voltage, the input is extremely tiny. We can therefore say that $\mathrm{V}_{3}$ approximately equals $V_{2}$. But pin 2 is tied to pin 1 so the output voltage essentially equals the input.

Inside the op amp we have an input offset voltage, $\mathrm{V}_{\text {osA }}$. The input offset voltage can be modeled by putting a voltage source in series with pin 3 . We then get

$$
\begin{equation*}
V_{1}=V_{3}+V_{o s A} \tag{6}
\end{equation*}
$$

For the LT1014, $\mathrm{V}_{\text {os }}$ can be as large as $\pm 0.3 \mathrm{mV}$.

Next look at op amp B in the ideal
 case. The voltage on pin 5 essentially equals the voltage on pin 6 .
$V_{6}=V_{5}$
Furthermore, the current flowing out of pin 6 is zero in this ideal case.

Note that the voltage across $\mathrm{R}_{4}$ is $\mathrm{V}_{6}$.
So I can say

$$
I_{R 4}=\frac{V_{6}}{R_{4}}
$$

But this current can only flow through $\mathrm{R}_{5}$. We can then say that the voltage across $\mathrm{R}_{5}$ equals $\mathrm{I}_{\mathrm{R} 4}$ times $\mathrm{R}_{5}$. The left end of $R_{5}$ is tied to pin 6 which we know is at the voltage $V_{6}$. Putting this all together we can say that

$$
\begin{gathered}
V_{7}=V_{R 5}+V_{6} \\
V_{7}=R_{5} I_{R 4}+V_{6} \\
V_{7}=R_{5} \frac{V_{6}}{R_{4}}+V_{6} \\
V_{7}=\left(1+\frac{R_{5}}{R_{4}}\right)\left(V_{6}\right)
\end{gathered}
$$

Since $V_{6}$ equals $V_{5}$ we can write

$$
V_{7}=\left(1+\frac{R_{5}}{R_{4}}\right)\left(V_{5}\right)
$$

Next consider the effect of input offset voltage, $\mathrm{V}_{\text {osB }}$. It can be put in series with pin 5 so modifies $\mathrm{V}_{5}$

$$
\begin{equation*}
V_{7}=\left(1+\frac{R_{5}}{R_{4}}\right)\left(V_{5}+V_{o s B}\right) \tag{7}
\end{equation*}
$$

I am ignoring the input bias current out of pin 6 here. Given an $R_{5}$ of 1 K and a maximum input bias current of 30 nA , this causes an error of $30 \mu \mathrm{~V}$ which is much less than the maximum input offset voltage. If it was a problem, I would put a 1 K in series with pin 5 . That would cancel the effects of input bias current. It would not address input offset current but that is smaller.


Op amp C swings between maximum and minimum output voltage. This is around 8 V . The typical gain of the op amp is $10^{5}$. This means that a change of $\frac{8 V}{10^{5}}=80 \mu \mathrm{~V}$ is all that is needed to swing the output over its maximum range. This is small enough to ignore. So we can say that the output of op amp C changes when the input equals about zero. But wait, we must include it's input offset voltage. So we end up with the state change somewhere within the input offset voltage tolerance of $\mathrm{V}_{\text {osc }}$. It is a maximum of $\pm 0.3$ mV at room temperature. Op amp D's inputs are tied to the same nodes as op amp C . When a voltage is applied to these inputs such that one op amp changes state, the other one will either change at the same time or have already changed state. It all depends on their input offset voltages. So I can limit my analysis to just the state change of op amp C.
$V_{o s C}=\left\{V_{10}\right\}-\left\{V_{9}\right\}$
But $V_{10}$ is the same as $V_{1}$ and $V_{9}$ is the same as $V_{7}$ so we can say

$$
V_{o S C}=\left\{V_{1}\right\}-\left\{V_{7}\right\}
$$

We know that
$V_{1}=V_{3}+V_{O S A}$
and

$$
\begin{equation*}
V_{7}=\left(1+\frac{R_{5}}{R_{4}}\right)\left(V_{5}+V_{O S B}\right) \tag{7}
\end{equation*}
$$

Plug them to get

$$
\begin{equation*}
V_{O S C}=\left\{V_{3}+V_{O S A}\right\}-\left\{\left(1+\frac{R_{5}}{R_{4}}\right)\left(V_{5}+V_{O S B}\right)\right\} \tag{9}
\end{equation*}
$$

We know
$V_{3}=\left(R_{3}+R_{x}\right) \times I_{x}$
And also
$V_{5}=R_{3} \times I_{x}$
Plug them into

$$
\begin{equation*}
V_{o S C}=\left\{\left[V_{3}\right]+V_{o S A}\right\}-\left\{\left(1+\frac{R_{5}}{R_{4}}\right)\left(\left[V_{5}\right]+V_{o S B}\right)\right\} \tag{9}
\end{equation*}
$$

And get
$V_{o s C}=\left\{\left[\left(R_{3}+R_{x}\right) \times I_{\chi}\right]+V_{o s A}\right\}-\left\{\left(1+\frac{R_{5}}{R_{4}}\right)\left(\left[R_{3} \times I_{\chi}\right]+V_{o S B}\right)\right]$
Then do a bit of algebra.
$V_{o S C}=\left[\left(R_{3}+R_{x}-R_{3}-\frac{R_{5} R_{3}}{R_{4}}\right) \times I_{x}\right]+\left[V_{o s A}-\left[\left(1+\frac{R_{5}}{R_{4}}\right)\left(V_{o S B}\right)\right]\right.$
$V_{o S C}=\left[\left(R_{x}-\frac{R_{5} R_{3}}{R_{4}}\right) \times I_{x}\right]+\left[V_{o S A}-\left[\left(1+\frac{R_{5}}{R_{4}}\right)\left(V_{o S B}\right)\right]\right.$
Note that $\left(1+\frac{R_{5}}{R_{4}}\right)=1.03$ multiplies $\mathrm{V}_{\text {osB }}$. I can change it to 1 with minimal effect on the accuracy of the equation.
$V_{o s C}=\left[\left(R_{x}-\frac{R_{5} R_{3}}{R_{4}}\right) \times I_{x}\right]+\left[V_{o s A}-V_{o S B}\right]$
Solving for $\mathrm{R}_{\mathrm{x}}$ we get
$R_{x}=\frac{R_{5} R_{3}}{R_{4}}+\frac{V_{o S A}-V_{o s B}-V_{o S C}}{I_{x}}$
All of these offset voltage are some value ranging between negative to positive so I can ignore their signs and just say
$R_{x}=\frac{R_{5} R_{3}}{R_{4}}+\frac{V_{o s A}+V_{\text {osB }}+V_{\text {os } C}}{I_{x}}$
Where $R_{x}$ is the threshold where op amp $C$ changes state.


If the total input offset voltage is zero, we get
$R_{x}=\frac{R_{5} R_{3}}{R_{4}}$
Plugging in what we know yields
$R_{x}=\frac{1 K \times 33 \text { ohms }}{160 K}$
$R_{x}=0.206$ ohms
But we really can't ignore the input offset voltages. If we go for absolute worst case, then we get

$$
\begin{align*}
& R_{x}=\frac{R_{5} R_{3}}{R_{4}}+\frac{V_{o s A}+V_{o s B}+V_{o S C}}{I_{x}}  \tag{11}\\
& R_{x}=0.206 \mathrm{ohms} \pm \frac{0.3 \mathrm{mV}+0.3 \mathrm{mV}+0.3 \mathrm{mV}}{50 \mathrm{~mA}} \\
& R_{x}=0.206 \mathrm{ohms} \pm 0.02 \mathrm{ohms}
\end{align*}
$$

Actual variation in the threshold should be less than this $\pm 10 \%$ tolerance.

## Extending this Idea

What if we accept a worst case error of $\pm 10 \%$ for the threshold but want to make the circuit more sensitive. We see that a test current of 50 mA lets us have a threshold of 0.2 ohms.

Keeping the voltage across $\mathrm{R}_{\mathrm{x}}$ the same, we can halve the threshold if we double the test current. So we would have an $R_{x}$ equal to 0.103 ohms. The test current would be 100 mA which means the tolerance on this threshold would be 0.01 ohms. We retain our error of $\pm 10 \%$.

In order to raise the test current to 100 mA , we would need to use equations 1 :

$$
\begin{equation*}
I_{x}=\frac{\left(V_{\text {battery }}-V_{E B s a t 1}\right)}{R_{2}+R_{x}+R_{3}} \tag{1}
\end{equation*}
$$

Again ignoring the effect of $R_{x}$ because it is much smaller than $R_{2}+R_{3}$,

$$
\begin{aligned}
& 100 \mathrm{~mA} \cong \frac{(9 \mathrm{~V}-0.75 \mathrm{~V})}{R_{2}+R_{3}} \\
& R_{2}+R_{3} \cong \frac{(8.25 \mathrm{~V})}{100 \mathrm{~mA}} \\
& R_{2}+R_{3} \cong 82.5 \mathrm{ohms}
\end{aligned}
$$

One design choice would be to set $\mathrm{R}_{2}$ equal to 56 ohms and $\mathrm{R}_{3}$ equal to 27 ohms. $\mathrm{R}_{2}$ would dissipate about 0.56 watts so should be a 1 watt resistor. $\mathrm{R}_{3}$ dissipates about 0.27 watts so should be $\mathrm{a}^{1 / 2}$ watt resistor. It would also be a good idea to lower $\mathrm{R}_{1}$ so Q1 doesn't have such a large base drive. Assuming a $\mathrm{V}_{\text {be }}$ of 0.75 V , an $\mathrm{R}_{1}$ of 27 ohms would mean it would pass 28 mA . That pulls about 22 mA out the base of Q1. This is a safe level of base current. R1 only dissipates 21 mW so can be an $1 / 8$ watt resistor.

Having a threshold of 0.103 ohms $\pm 10 \%$ is attractive but that 100 mA test current pushes us deeper into the unknown with respect to damaging bearings. This is why I developed the Model 2 which has a threshold of 0.01 ohms and a test current of less than 25 mA :
http://rick.sparber.org/LEEF_Model_2.pdf

I welcome your comments and questions.
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[^0]:    ${ }^{1}$ You are free to copy and distribute this document but not change it.

[^1]:    ${ }^{2}$ This is called a Kelvin connection.

